# Benelux Algorithm Programming Contest (BAPC) preliminaries 2025

Solutions presentation

The BAPC 2025 Jury October 4, 2025

Problem author: Mike de Vries

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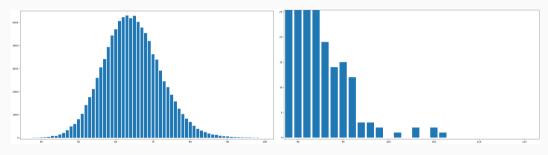
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**Running time:**  $\mathcal{O}(nq)$  for q commands.

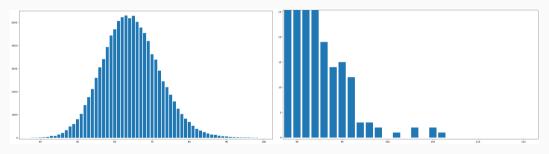
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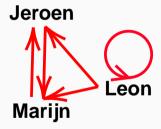
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**Issue:**  $n = 10^5$ , so we need an  $\mathcal{O}(n)$ -time solution.

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**Solution:** • Loop through all nodes, and run a DFS if not yet visited.

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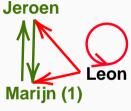
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• Check whether this is true using a DFS, starting from this last node.

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**Problem:** There is a sequence of real numbers  $a=(a_1,\ldots,a_n)$  with  $a_1+\cdots+a_n=100$  and  $a_1\geq\cdots\geq a_n\geq 0$ . Given a subset  $\{a_i\}_{i\in S}$  of these numbers, determine maximal lower bounds  $I_1,\ldots,I_n$  and minimal upper bounds  $r_1,\ldots,r_n$  such that

$$I_i \le a_i \le r_i$$
 for  $1 \le i \le n$ .

E.g., with 
$$a = (60, ?, ?, 5, ?)$$
:

spam

egg

sausage

bacon

5

tomato

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**First observation:** Since a is nonincreasing, it is immediate that  $a_i$  satisfies  $l_i' \leq a \leq r_i'$  with

$$l_i' = \max\{\ a_j\colon j \geq i, j \in S\} \qquad r_i' = \min\{\ a_j\colon j \leq i, j \in S\}.$$
 spam 
$$\qquad \qquad a_1 = 60$$
 
$$\qquad \text{egg} \qquad \qquad 5 \leq a_2 \leq 60$$
 sausage 
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 bacon 
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 tomato 
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Implementation: These values can be computed in linear time by first computing

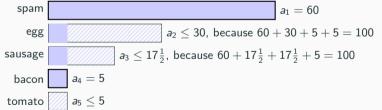
$$\operatorname{prev}(i) = \max\{j \in S : j < i\}, \quad \operatorname{next}(i) = \max\{j \in S : j > i\},$$

preferably with useful boundary values, for instance by introducing  $a_0 = 100$  and  $a_{n+1} = 0$ . Then, for  $i \notin S$  we have  $l'_i = a_j$  with j = next(i) because a is decreasing.

Fix upper bounds: For  $i \notin S$ , the (unknown) amount  $a_i$  satisfies  $l_i' \le a_i \le r_i'$ , but we know more: Assuming all other amounts attain their *lower* bound, then their sum cannot exceed 100, so we have the constraint

$$\left(\sum_{j< i} \max(a_i, l_j')\right) + a_i + \sum_{j> i} l_j' \leq 100\,,$$

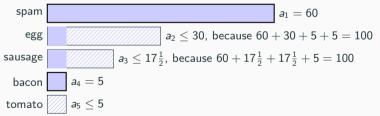
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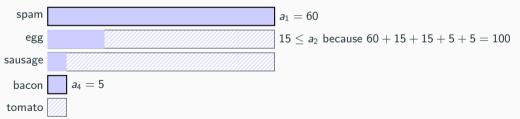


**Implementation:** To determine max  $a_i$ , use binary search in the interval  $[l'_i, r'_i]$  or rewrite the constraint for closed formula.

**Fix lower bounds:** Symmetrically, assuming all other amounts attain their *maximum* bound, then their sum must be at least 100, so we have the constraint

$$\left(\sum_{j< i} r'_j\right) + a_i + \sum_{j>i} \min(a_i, r'_j) \geq 100,$$

Can solve for the smallest  $a_i$ .



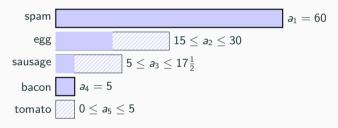
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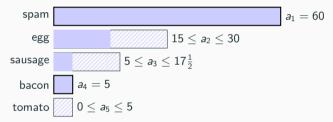
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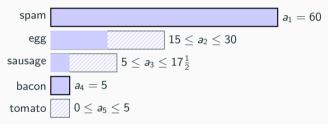
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### A: Alto Adaptation

Problem author: Arnoud van der Leer, Maarten Sijm

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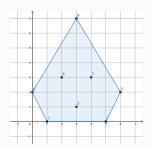
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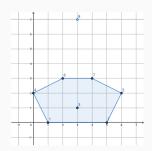
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**Possible solution:** Create *k* numbers/variables using single characters, starting with zeros. Put the remaining characters in the last token, making sure to start with letters, then non-zero digits. Sorting makes it easier, but is not strictly necessary.

00123abcd ightarrow 0, 0, 1, 2, dcba3 000000001 ightarrow 0, 0, 0, 0, 10000

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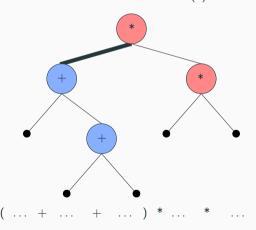
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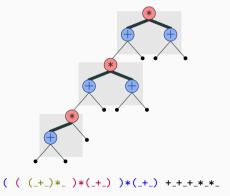
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**Solution:** Greedily construct as many (\_+\_)\*(\_+\_) patterns as possible, use (\_+\_)\*\_ to get rid of a single pair of parentheses, and put all remaining operators at the end.



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**Complete solution:** Count the parentheses, operators, zeros, and other digits/letters, and check all edge conditions. Construct tokens. Then greedily construct the expression's structure, and fill in the tokens.

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- The minimum<sup>1</sup> number of lines the jury needed to solve all problems is

$$4+2+6+1+4+11+3+2+5+2+1+7=48$$

On average 4 lines per problem, down from  $16\frac{1}{4}$  in last year's preliminaries<sup>2</sup>

<sup>&</sup>lt;sup>1</sup>With mostly™ PEP 8-compliant code golfing

<sup>&</sup>lt;sup>2</sup>But we did way less golfing last year

#### Thanks to:

# The proofreaders

Arnoud van der Leer

Dany Sluijk

Geertje Ulijn

Jaap Eldering Kevin Verbeek

Michael Zündorf

Pavel Kunyavskiy Kotlin Hero

Tobias Roehr 🎈

Thomas Verwoerd

Wendy Yi

# The jury

Ivan Fefer

Jeroen Op de Beek

Jonas van der Schaaf Lammert Westerdijk

Leon van der Waal

Maarten Siim

Marijn Adriaanse

Mike de Vries

Ragnar Groot Koerkamp

Reinier Schmiermann

Thore Husfeldt

Wietze Koops

Want to join the jury? Submit to the Call for Problems of BAPC 2026 at:

https://jury.bapc.eu/